Lecture for 3rd-year students, Chemistry dept.



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#### 「放射線を科学的に理解する

— 基礎からわかる東大教養の講義 —」

鳥居寛之・小豆川勝見・渡辺雄一郎 著 中川恵一 執筆協力

#### **丸善出版** 本体 2500円+税

1章 放射線とは?《放射線入門》
2章 放射線の性質《放射線物理学Ⅰ》
3章 原子力発電で生み出される放射性物質 《原子核物理学・原子力工学》
4章 放射線量の評価《放射線物理学Ⅱ》
5章 放射線の測り方《放射線計測学》
6章 環境中での放射性物質《環境放射化学》
7章 放射線の細胞への影響《放射線生物学》
8章 放射線の人体への影響《放射線医学》
9章 放射性物質と農業《植物栄養学・土壌肥料学》
10章 放射線の防護と安全《放射線防護学》
11章 役に立つ放射線《放射線の利用・加速器科学》

放射線を理解するには、物理学・化学・生物学・医学・工学など 多くの分野の知識が必要です。しかしこれらすべてを網羅すること は難しく、系統立てて学べる機会は非常に少ないのが実情です。 本書は東京大学教養学部で行われた講義をもとに、放射線につい て多角的に学べるよう配慮しています。日常生活や原発事故にかか わる具体的な例を引きながらやさしくていねいに解説しましたので 高校生や一般の方にも広く読んでいただきたいと願っています。

http://radphys4.c.u-tokyo.ac.jp/~torii/lecture/radiolect-kn.html

Lecture for 3rd-year students, Chemistry dept.



5<sup>th</sup> lecture Interaction between radiation & matter (I)

# 鳥居 寛之 (Hiroyuki A. TORII)

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Billet de 500 Francs Français en circulation: 1993–1999

α-rayhelium nucleusβ-rayelectronγ-rayphoton (EM wave)X-rayphoton (EM wave)





#### Interaction between radiation and matter Slowing-down of charged particles 荷電粒子の減速

#### Penetration of radiation



Slowing-down and energy loss of 荷電粒子の減速 charged particles (α-ray, β-ray etc.)<sup>(エネルギー損失)</sup>

Step-by-step energy loss due to ionization and excitation of atoms / molecules.

Fixed range of the same heavy particles for a given energy. (with a slight deviation)

**Stopping power** = energy loss per unit length =  $-\left\langle \frac{dE}{dx} \right\rangle$ 

#### Attenuation of photons (X-ray, Y-ray) 光子の減衰(減弱)

Photons are lost by stochastic processes of absorption or scattering, but the rest remain intact through.



#### **Exponential decrease of photon number**

reaction cross section  $\sigma$  is proportional to the reaction probability per unit length.

# **Energy loss of charged particles**





## Along the track after passage of charged particles



Ions and excited atoms are produced, while energetic secondary electrons can ionize other atoms.
X-rays are emitted after atomic recombination or deexcitation.

Atomic ionization & excitation **Deexcitation of excited atoms** X ray, UV & visible lights **Recombination of ions & electrons Scintillation light** Breakage of chemical bonds fluorescence of atoms & molecules excited by radiation **Recombinaton of chemical bonds Generation of free radicals &** activated molecules **Damages to DNAs** 

## Stopping power (Energy loss, Linear Energy Transfer : LET)

阻止能

(エネルギー損失、線エネルギー付与)



#### Charged particle : Coulomb force

Kinetic energy of the particle is transferred to <u>a number of</u> <u>electrons</u> (secondary electrons) scattered via ionization or excitation of atoms and molecules in the matter. The particle loses its energy and is <u>slowed down</u> (electron collision stopping power).

 heavy particles : proton beams, α-rays, heavy ions, pions, muons Small energy transfer to each single electron. Slowed down via scattering of many electrons. Small momentum transfer results in almost linear trajectory.
 light particles : electrons (e<sup>-</sup>), positrons (e<sup>+</sup>) Large energy transfer per single collision. Sometimes zig-zag trajectories. Can generate secondary electrons with large kinetic energy (δ-rays).

#### **Tracks of α-ray** α 7.7 MeV Radiation 7.7 MeV 0.1 cm a observed by cloud chambers 0.2 MeV 0.2 MeV b 1 cm β**--ray** 0.056 MeV 0.056 MeV 1 cm С **Y-ray** 8 0.047 MeV 0.047 MeV 1 cm d

**Figure 7.5** Cloud chamber tracks of  $\alpha$ ,  $\beta$ , (e<sup>-</sup>), and  $\gamma$ -rays at 1 bar in air ((a), (b), and (c)) and in methane (d). (*From W. Gentner, H. Maier-Leibnitz, and H. Bothe.*)



# Stopping power

energy loss

**Charged particle : Coulomb force** 

Kinetic energy of the particle is transferred to <u>a number of</u> <u>electrons (secondary electrons) scattered</u> via ionization

or **excitation** of atoms and molecules in the matter. The particle loses its energy and is <u>slowed down</u> (**electron collision stopping power**).

Energies transferred to nuclei are relatively small, because they are heavy. (Nuclear collision stopping power is usually negligible.)

Among secondary particles (mostly **secondary electrons**), those with rather <u>high energy</u> and capable of <u>ionizing</u> atoms and molecules are sometimes called  $\delta$ -rays.

Number of ionizations (electron-ion pairs) per unit length = Specific ionization
Stopping power / Specific ionization = W-value
W-value : Average energy required to produce 1 ion pair.
Does not depend on species or energy of charged particles.
Value larger than the ionization energy (due to loss by excitation).
W ~ 30 eV not depending on the material.



r

#### 阻止能 Stopping power for charged particles

**ノIOSS** Linear Energy Transfer : LET (エネルギー損失、線エネルギー付与)

#### **Bohr's calculation**

Equation modified along with the SI units

$$-\left\langle \frac{dE}{dx} \right\rangle = \frac{z^2 e^4}{4\pi \epsilon_0^2 m_e v^2} n_e \ln \frac{b_{\text{max}}}{b_{\text{min}}} \quad \text{on blackboard}$$
Bethe-Bloch equation
$$-\left\langle \frac{dE}{dx} \right\rangle = K z^2 \frac{Z}{A} \frac{1}{\beta^2} \left[ \frac{1}{2} \ln \frac{2m_e c^2 \beta^2 \gamma^2 T_{\text{max}}}{I^2} - \beta^2 - \frac{\delta(\beta\gamma)}{2} \right]$$

$$K = 4\pi N_A r_e^2 m_e c^2 \rho \qquad Z/A \approx 1/2 \text{ except for hydrogen.}$$
Does not depend very much on the material mass stopping power
$$-\frac{1}{\rho} \left\langle \frac{dE}{dx} \right\rangle \propto \frac{z^2}{v^2} = \frac{z^2 M/2}{Mv^2/2} \propto \frac{z^2 M}{T}$$

energy loss

# Stopping power of materials for charged particles



Mass stopping power does not depend very much on the material.

#### Stopping power for various charged particles in air







## Stopping power (Energy loss, Linear Energy Transfer : LET) 阻止能 (エネルギー損失、線エネルギー付与)

proton beams, α-rays, heavy ions : high-LET radiation neutron beams : give high LET by <u>kicking out protons</u> in media.
β-rays (electron beams) : low-LET radiation
photons (X-rays, γ-rays) : <u>kick out electrons</u> in media.
or create electron-positron pairs at high energies, giving low LET.

Does not depend very much on the material.

mass stopping power 
$$\frac{1}{\rho} \left\langle \frac{dE}{dx} \right\rangle \propto \frac{z^2}{v^2} = \frac{z^2 M/2}{Mv^2/2} \propto \frac{z^2 M}{T}$$
  
MeV / (g / cm<sup>2</sup>)

#### Range of various charged particles in air



Integral of the reciprocal of the stopping power. Range proton beams, α-rays, heavy ions : short range Shielding is easy against external exposure. **neutron beams :** penetrate deep into matter. do not interact with electrons. drastic deceleration by collision with protons in media. (but the cross section / reaction probability is small.) Long range. Shielding by materials including H atoms.  $\beta$ -rays (electron beams) : longer range than p,  $\alpha$ , ions. easily scattered by electrons in media.

Does not depend very much on the material.

mass stopping power 
$$\frac{1}{\rho} \left\langle \frac{dE}{dx} \right\rangle \propto \frac{z^2}{v^2} = \frac{z^2 M/2}{Mv^2/2} \propto \frac{z^2 M}{T}$$



**Figure 7.4** Absorption curve for <sup>32</sup>P  $\beta$ -radiation showing extrapolated ( $C_4$ ) and average ( $C_3$ ) ranges. The dashed curve is obtained after subtraction of background.

# **Range** Integral of the reciprocal of the stopping power. Shielding is easier for radiation with smaller interaction.



## **Exposure to different radiations**

- α-ray: a few cm of range in the air. Stops at surface cells of organism.
   Internal exposure needs attention : all the energies are given to cells within a short range.
- β-ray : external exposure to the skin & internal exposure need attention.
- γ-ray : penetrates through the body, some without any interaction while the others with some interaction X-ray (photoelectric effect / Compton scattering) and get absorbed inside the body. The interior of the body are equally exposed to radiation even in the case of external exposure.
- X-ray : analogous to γ-ray. Part of the energies are absorbed.



#### Radioactive contamination map

((...))

# What does otective clothi

#### protective clothing 放射線防護服 protect ?

早川由紀夫教授(群馬大学)作成、7月26日版

さいたま。

東京(新宿

三訂版7月26日 (初版4月21日) 等値線作成:早川由紀夫(群馬大学)(kipuka.blog70.fc2.com/) @nnistarさんの地図 (www.nnistar.com/gmap/fukushima.html) Contour lines drawn by Yukio Hayakawa (Gunma Univ.), Source: @nnistar 地図製図:萩原佐知子

背景地図には電子国土ボータル (portal.cyberjapan.jp)の地図を使用しました。

Protons, alpha-particles and ions have their uniform ranges as a function of their energy. Electrons (beta-particles) are subject to scattering. The range measured as the rectilinear distance (or the material thichkness) has a large dispersion.

Neutrons and photons attenuate exponentially with depth, as the reaction occurs stochastically.



# Radiation therapy<br/>for cancerMultiple irradiation of a few Gy each.X-rayheavy ion beam (Carbon ions)





proton beam pion beam (antiproton beam)



#### e.g. prostate cancer (前立腺がんの例)

**4-port irradiation** 

3D-CRT (three-dimensional conformal radiotherapy)

IMRT : Intensity-Modulated () Radiation Therapy

前後左右4門照射



強度変調放射線治療



- 前立腺の他に、膀胱や直腸が 高線量域に含まれる
- 70Gyが限界(難治性の晩期 粘膜障害の発現を許容範囲 に抑えるためには、実際には 60~66Gy程度が限界となる)



- 前立腺に線量が集中し、膀胱や直腸への線量が低く抑えられる
- 70Gy以上の投与が可能であるが、線量の集中に限界があり、線量増加に伴う副作用の増加が懸念される



- 前立腺への集中性がさらに 強化
- IGRTを併用することで、3次
   元原体照射を超える高線量
   を安全に投与することが可能

外照射法の進歩を背景に、前立腺癌に対する線量増加効果が積極的に検討されている。









#### 前立腺IMRTの線量分布

#### Interaction between radiation and matter 放射線と物質との相互作用 **Attenuation of photons**





### Interaction relating to photons (X-ray, γ-ray)



A photon kicks **one electron** out of an atom. The photon is absorbed.

A photon is **scattered by one electron**. The photon loses a large fraction of its energy. A photon with more than a MeV energy produces electronpositron pair.

#### A charged particle emitts a photon when they are abruptly decelerated or when their trajectory is curved.

#### Generation of high-energy electrons

(same particles as  $\beta$ -ray)







#### Bremsstrahlung

制動放射



Charged particles emit photons (X-ray) when their velocity is abruptly changed (i.e. decelerated or their orbits are curved).  $\Delta E \propto Z^2$ 

 $\beta$ -rays should not be stopped with lead.

bremsstrahlung : energy loss Srad

Srad	$(E+mc^2) Z$
Scol	$-\frac{1600 mc^2}{1600 mc^2}$

Pb (lead; Z = 82)  $\frac{S_{\text{rad}}}{a} \approx \frac{EZ}{a} \approx \frac{E/\text{MeV}}{a}$  $S_{\rm col}$  800 MeV

 $\beta$ -rays should not be stopped with lead.

Bremsstrahlung is negligible compared with stopping power by electron collision, unless the energy is more than the order of a GeV.



#### cosmic ray

#### electromagnetic shower

#### Material dependence of photon cross sections



photoelectric effect  $\propto Z^{4\sim5}$ Compton scattering  $\propto Z$ bremsstrahlung  $\propto Z^2$ 



#### **Röntgen radiography**

国立循環器病センター 内藤博昭先生のスライドより借用





5

4

**P-2**;  $\mu_3 + \mu_4 = 9$ **P-3**;  $\mu_1 + \mu_3 = 6$ 

**P-4**;  $\mu_1 + \mu_4 = 5$ 

Transmission用

検出器

ピクセル (画素)

断面

ボクセル

(体積素)

Emission用

検出器

#### X線検査用造影剤

* 陽性造影剤	元素	原子番号	K吸収端
•ヨード造影剤:血管造影用	Т	53	33.16 keV
・硫酸ベリウム:消化管造影用	Ва	56	37.41 keV
・キセノン ガス(脳血流CT)	Хе	54	34.56 keV
* <mark>陰性造影剤</mark> ・気体:空気, 酸素, 炭酸ガス ・オリーブ油(膀胱CT)	ヨード 造影評 CH,CHC OH イオノ		HCH ✓I CONHCH ✓CH₂OH CONHCH ✓CH₂OH CH₂OH CH₂OH







写真提供:放射線医学総合研

contrast media (**I**, **Ba**, **Xe**) : large **Z** = large attenuation

タングステンの特性X線 X線の発生と減弱 非漏沼 X線の相対強度 特件X線 1.000 -200kV 制動放射 (量減弱係数 100 (一吸収端 X線光子のエネルギー(keV) 10.0 ヨード \*光電効果:光電吸収 元素のK吸収端(keV): 1.0 骨 H 0.0136, C 0.283, O 0.531 筋肉 \* コンプトン散乱:非弾性散乱 0.1 40 60 80 100 120 140 20 光子エネルギー(keV)



# Attenuation and absorption of photons (γ-ray) in material.

#### Exponential decrease of photon number

Photoelectric effect, Compton scattering &c. are stochastical processes.  $\frac{\mathrm{d}\Phi(x)}{\mathrm{d}x} = -\mu\,\dot{\Phi}(x)$  $\dot{\Phi}(x) = \dot{\Phi}(0) e^{-\mu x}$ ln *x* : natural logarithm.  $\check{\Phi}(L) = \check{\Phi}(0) / 2$  $L = \ln 2 / \mu$  $\equiv \log_e x$  $\Phi$  : particle fluence rate for  $\gamma$  ( $h\nu = 0.66$  MeV) from <sup>137</sup>Cs  $L^{\rm air} = 69.2 \, {\rm m}$ x: distance, L: half-value thickness  $\mu^{air} = 0.0100 \text{ m}^{-1}$  $\mu$ : linear attenuation coefficient  $(\mu/\rho)^{air} = 0.077 (g/cm^2)^{-1}$  $\mu/\rho$ : mass attenuation coefficient  $\mu_{\rm en}/\rho < \mu/\rho$  $(\mu_{en}/\rho)^{water} = 0.033 (g/cm^2)^{-1}$  $\mu_{en}/\rho$ : mass energy-absorption coefficient *H* : equivalent dose rate ( = absorption dose rate for  $\gamma$ -ray )  $\dot{H} = h\nu (\mu_{en}/\rho) \dot{\Phi}$ ,  $h\nu (\mu_{en}/\rho)^{water} = 3.5 \times 10^{-16} \,\mathrm{Sv} \,\mathrm{m}^2$ 









*p*: surface density of radioactivity [Bq/m<sup>2</sup>]

$$\mathbf{\dot{H}}$$
: equivalent dose rate [Sv/s]  $\dot{H}/\dot{\Phi} = h\nu (\mu_{\rm en}/\rho) = 3.5 \times 10^{-16} \, {\rm Sv} \, {\rm m}^2$ 

$$\int_{0}^{L^{\text{air}}} \frac{x}{x^{2} + h^{2}} \, \mathrm{d}x = \frac{1}{2} \ln \left( x^{2} + h^{2} \right) \Big|_{x=0}^{L^{\text{air}}} = \frac{1}{2} \ln \left[ \left( \frac{L^{\text{air}}}{h} \right)^{2} + 1 \right]$$

 $L^{\rm air} = 69.2 \, {\rm m} \qquad h = 1 \, {\rm m}$ 

+ Build-up effect due to Compton scattering (ca. + 50%) <sup>137</sup>Cs : 2.1 (μSv/h) / (MBq/m<sup>2</sup>) .... calculation by IAEA

Problem with decontamination : half of the dose due to soil contamination of distance 10–100 m.

Radioactive contamination map : aerial monitoring by MEXT



http://radioactivity.mext.go.jp/ja/1910/2011/11/1910\_1125\_2.pdf <sup>137</sup>Cs: 2.1 (μSv/h) / (MBq/m<sup>2</sup>) .... calculation by IAEA

30

岩手秀

Cs-134 BU Cs-137 0

600k - 1000k 300k - 600k 100k - 300k

100

60k - 100k

背景地図:電子図:

30k - 60k 10k - 30k ≤ 10k

合計の沈着量

## neutron reaction and activation

#### Elastic scattering of neutrons

**Fast neutrons** slow down by repeated **collision with nuclei.** Each collision decreases the energy exponentially.

Neutrons are most **effectively decelerated** by collision **with protons** having the same mass.

Neutrons are effectively shielded by water or concrete containing hydrogen atoms.

Scattered nuclei such as protons (charged high-LET particles) ionize atoms & molecules.

#### Absorption of neutron and nuclear reaction

After having formed a nucleus with a mass number larger by unity, the formed unstable nucleus often emits e.g. a  $\gamma$ -ray, leaving radioactive nuclide, thus resulting in **activation**.

#### **Activation** 放射化

For non-radioactive materials to obtain radioactivity by irradiation of radiation.

Radioactive nuclides can be created via nuclear reactions by **neutrons**, or by γ-rays with energies over 10 MeV.

 $\beta$ -rays or  $\gamma$ -rays from radioisotopes nor X-rays from atoms can cause activation. Be careful with activation in radiation control areas such as accelerator facilities and nuclear reactors.

# Radiation chemistry 放射線化学

Number of ionizations (electron-ion pairs) per unit length = Specific ionization
Stopping power / Specific ionization = W-value
W-value : Average energy required to produce 1 ion pair.
Does not depend on species or energy of charged particles.
Value larger than the ionization energy (due to loss by excitation).
W ~ 30 eV not depending on the material.

#### G-value : radiation chemical yield :

The G value refers to the number of molecules of reactant consumed or product formed per 100 eV of energy absorbed. Normally the number is up to 10, but it can sometimes be huge in the case of a chain reaction.

#### Elementary reactions induced by radiation (selected)

$$AB \longrightarrow AB^{+} + e^{-}$$
$$AB \longrightarrow AB^{*}$$

$$AB^{+} + e^{-} \rightarrow AB^{*}$$
$$AB^{*} \rightarrow A \cdot + B \cdot$$

ionization excitaion

recombination formation of radicals

#### **Reactions in water**

oxygen effect

 $H_2O \longrightarrow H_2O^+ \cdot + e^-$ **HO**<sub>2</sub>.  $H_2O \longrightarrow H_2O^*$ (hydroperoxyl radical) (hydroxyl radical)  $O_{2}^{-}$  $H_2O^+ \cdot + H_2O \rightarrow H_3O^+ + \cdot OH$ (superoxide anion)  $e^{-}(+ n H_2O) \rightarrow e^{-}aq_{(hydrated)}$ (hydrogen peroxide) electron)  $H_2O^* \rightarrow H \cdot + \cdot OH$ (active oxygen)  $H_3O^+ + e_{aq}^- \rightarrow H_{aq}^- + H_2O$ (hydrogen radical)

<b>Reactions in water</b> (G-value) by γ-ray.	d
$H_2O \longrightarrow H_2O^+ \cdot + e^-$	ionization
$H_2O \longrightarrow H_2O^*$ $G(\cdot OH) = 2.7$	excitation
(hydroxyl radical) $H_2O^+ \cdot + H_2O \rightarrow H_3O^+ + \cdot OH$ $e^- (+ n H_2O) \rightarrow e^{aq}$ (hydrated electron) $H_2O^* \rightarrow H \cdot + \cdot OH$ $H_3O^+ + e^{aq} \rightarrow H \cdot + H_2O$ (hydrogen radical) $G(H \cdot) = 0.55$	• ion-molecule reaction production of hydrated electron dissociation (production of radicals) electron capture
$H_2O^+ + e^- \rightarrow H_2O^*$	recombination
$\cdot OH + e_{aq}^{-} \rightarrow OH^{-}$	electron capture
$H_2O^* \rightarrow H_2O$	deexcitation
$H \cdot + H \cdot \rightarrow H_2  G(H_2) = 0.45$	production of molecule
$\cdot OH + \cdot OH \rightarrow H_2O_2  G(H_2O_2) = 0.7$	production of molecule
$H \cdot + \cdot OH \rightarrow H_2O$	production of molecule



#### Graft polymerization by irradiation of e<sup>-</sup> beam or γ-ray.



A braid adsorbent having the functional group of amidoxime is a promising material for the recovery of uranium. 図2 放射線グラフト重合によるウラン捕集材の合成法

[出典]片貝 秋雄、瀬古 典明、川上 尚志、斉藤 恭一、須郷 高信、原子力学会誌 40(11)、879(1998) Synthesis of uranium-adsorbent by means of graft polymerization by irradiation of radiation.

#### **Radiation-induced cross-linking reaction**





#### **Application in industry**

#### O<u>ラジアルタイヤ、耐熱電線</u> radial tires

ラジアルタイヤは、有機繊維で補強されたゴムで高圧に耐えられる構造 になっています。成形器で熱と圧力を加えてタイヤの形にしますが、この 時、繊維補強ゴムは大きな変形を受け、補強繊維のずれやはみ出しが おきやすくなります。これを防ぐため、繊維補強ゴムに電子線を照射して 強度を上げます。(市場規模:平成15年度1兆円)

また、電線の被覆に使われているゴムやプラスチックはそのまま熱を加 えると溶けて流れ落ちます。電子線を照射すると熱を加えても溶けにくくな ります。

#### heat-resistant electric wires

#### semiconductors 〇半導体

IC(集積回路)の回路のパターンの線は髪の毛の太さの50~100分の1で あり、その細工をするためにリソグラフィといった技術が使われる。リソグラ フィは版画の技術のようなもので、半導体表面に光や放射線を当てると化 学変化する感光剤を塗り、加工したい形状に切り抜いた板(マスク)をのせ て放射線を当てて、マスクの型どおりに加工するもの。イオンビームや中性 子ビームを利用した不純物導入等も行っています。

(市場規模:平成15年度6.3兆円)

#### 〇発泡材料(緩衝材料、断熱材料)

お風呂場で使うバスマット、あるいはプールで使うビート板に使用されて いる発泡ポリエチレンをご存じですか。あの防水性、浮力が高く、ほどよ く硬い素材 は、ポリエチレンに放射線を照射し、加熱することで内部に細 かい気泡をつくりだしたもので、これもいまから20年以上も前に開発され た素材です。 foamed materials



ラジアルタイヤ、耐熱電線



半導体



#### Lecture slides

#### http://radphys4.c.u-tokyo.ac.jp/~torii/lecture/



#### **Contact address**

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### 担当教員:鳥居 寛之 Lecturer : Hiroyuki A. TORII

Fine. Per oggi è tutto. Fini pour aujourd'hui That's all for today. Всё за сегодня. 오늘은 이만 마치겠습니다. 今天就学到这儿了。

Ci vediamo la prossima settimana. On se voit la semaine prochaine. See you next week. Увидимся на следующей неделе. 다음 주에 또 만납시다. 下周见。